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Accuracy enhancement of biometric recognition using iterative weights optimization algorithm



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Abstract

A new approach is proposed to quantitatively evaluate the binary detection performance of the biometric personal recognition systems. The importance of correlation between the overall detection performance and the area under the genuine acceptance rate (GAR) versus false acceptance rate (FAR) graph, commonly known as receiver operating characteristics (ROC) is recognized. Using the ROC curve, relation between GAR_{min} and minimum recognition accuracy is derived, particularly for high security applications (HSA). Finally, effectiveness of any binary recognition system is predicted using three important parameters, namely GAR_{min}, the time required for recognition and computational complexity of the computer processing system. The palm print (PP) modality is used to validate the theoretical basis. It is observed that by combining different useful feature-extraction techniques, it is possible to improve the system accuracy. An optimum algorithm to appropriately choose weights has been suggested, which iteratively enhances the system accuracy. This also improves the effectiveness of the system.

Keywords: False acceptance rate (FAR), Genuine acceptance rate (GAR), Receiver operating characteristics (ROC), Area under the curve (AUC), Score level summing, Optimal weights algorithm (OWA)

1 Introduction

Extensive work has been done in the area of biometric recognition using different traits such as face, finger print, iris, voice, different hand-based modalities, gait, etc. [1-4]. However, unimodal systems have their own advantages and limitations. They require only one sensor to acquire data. Therefore, the data acquisition becomes less expensive and more user-friendly. They also require limited signal processing time and less computational efforts. However, the performance of any unimodal system gets degraded due to several reasons like erroneous database, spoofing attacks, etc. [5–7]. The unimodal systems provide lower values of genuine acceptance rate (GAR) and low to middle range of accuracies [8-10]. The proposed work in this paper focuses on increasing this low value of minimum value of genuine acceptance rate (GAR_{min}) for unimodal systems, with a view to boost their accuracies. This is done using mathematical modeling of signal detection performance and derivation of accuracy in terms of GARmin for high security applications (HSA). In this paper, efforts are made for enhancing the accuracy of palm print (PP)-based recognition using different feature extraction techniques, such as use of different discrete wavelet transform (DWT) coefficients and combinations of different DWT coefficients. Compared to other traits, PP features have certain distinct advantages. PP modality provides reasonably good recognition accuracy. PP authentication ensures advantages such as very stable line features, low intrusiveness, and requires low resolution imaging. As the palm area is much larger, more distinctive features can be captured. [11–13].

The GAR_{min} decides the detection performance of the system. The paper clearly brings out the correlation between the system accuracy with area under the curve (AUC) of its "GAR versus FAR characteristics," commonly known as receiver operating characteristics (ROC) of the system. In order to validate theoretical concepts proposed, PP modality is used. For PP modality, various feature

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extraction techniques are used to increase AUC of its ROC characteristics. Further, an appropriate iterative optimal weights algorithm (OWA) is suggested to further enhance the accuracy of the system. Finally, effectiveness of any binary recognition system is computed in terms of GARmin, recognition time, and computational complexity.

The paper is organized as follows: after brief introduction, Section 2 outlines the work done by other researchers in this field. Section 3 is devoted for mathematical background for binary signal detection and definition of effectiveness of the system. Section 4 elaborates the proposed methodology for the biometric image data acquisition, feature extraction, and feature mapping. Section 5 includes the system effectiveness calculations, analysis of the recognition performance, and the discussions on results, followed by conclusions.

2 Related work

Researchers have used different biometric traits for personal recognition purposes. As our focus is mainly on enhancing accuracy of unimodal hand-based systems, we have briefly reviewed research efforts, which reflect accuracies obtained for specific hand-based modalities.

E. Wong et al. (2008) [14] and M. Dale et al. (2009) [15] have worked on PP-based biometric recognition. They have reported accuracy levels of 94.84% and 97% respectively. Zhenhua Guo et al. (2011) [16] have used (2D) PCA for PP feature extraction. They have obtained an accuracy of 97.43%. Goh Kahong Michael et al. (2012) [17] have described a contactless hand-based biometric system. They have extracted features using directional coding techniques, and normalized hamming distance has been used to find similarity between two feature sets. For individual modality, they have obtained GAR of 0.89 for hand geometry, 0.95 for PP, 0.75 for knuckle finger print, and 0.96 for finger vein modality. Kuang-Shyr Klu et al. (2013) [18] have used directional filter bank for palm vein modality in their work. They have quoted an accuracy of 99%. Sibi Sasidharan et al. (2015) [19] have presented a paper in which they have given analysis of various methods and algorithms that identify the vein patterns for authentication purpose. They have concluded that palm vein recognition using neural network to be quite efficient and accurate. Raghavendra et al. (2015) [20] have explored the idea of PP recognition using a sparse representation of features obtained from Bank of Binarized Statistical Image Features (BSIF). Bank of BSIF that comprises of 56 different Bank of BSIF filters whose responses on the given PP modality image is processed independently and classified using sparse representation classifier (SRC). In the given PP sample, they obtained response on each of the Bank of BSIF filter and then they obtained the corresponding comparison score using SRC. Finally, they have selected the best comparison score that corresponds to the minimum value of the residual error. S. Khellat-Kihel et al. (2016) [21] have mentioned GAR values of 0.927, 0.846, 0.547 for finger knuckle print, finger vein, and fingerprint modalities respectively. Kunal Kumar et al. (2016) [5] have presented the strengths and weakness of selected biometric mechanisms and recommend novel solutions to include in multimodal biometric systems to improve on the current biometric drawbacks. Gopala et al. (2016) [6] have proposed fusion of PP, palm-phalanges print (PPP), and dorsal hand vein (DHV) in their paper. They have obtained GAR of 94% for PP, 98.2% for PPP, 92% for DHV, and GAR of 99.6% for score level fusion of PP-PPP-DHV. They have implemented score level fusion with conventional operators like Yager's ordered weighted averaging (OWA) operator and t norm fusion operator. Shital Baghel et al. (2017) [7] have mentioned the drawbacks of unimodal systems compared to multimodal systems. Gopal Chaudhary et al. (2017) [8] have developed system using biometric trait, PPP. They have used different feature extraction techniques such as histograms of oriented gradients, Gaussian membership function (GMF) feature, mean value, and average absolute deviation method. Anchal Bansal et al. (2018) [9] have presented a review of different features of fingerprint recognition systems. The invariant and discriminatory information present in the fingerprint images are captured using fingerprint ridges known as minutiae. They have compared pattern recognition-based approach with wavelet-based approaches. Rupali L. et al. (2014) [22] have proposed the score level fusion of face and fingerprint modalities. Minutiae matching and Gabor filter techniques have been used for fingerprint recognition and principal component analysis for face recognition. After performing score normalization, score level fusion was done using simple sum rule. They have quoted an overall accuracy of 97.5% with FAR and FRR of 1.3% and 4 .0 1% respectively. Assuming occurrence of equiprobable hypotheses, this represents a percentage accuracy of approx. 97.235%. Furthermore, FAR level mentioned makes this approach not at all suitable for HSA, which is the prime focus of the present paper. Kamer Vishi et al. (2017) [23] have combined the normalized scores obtained from finger-veins and fingerprints modalities using different score level fusion techniques. They have implemented four score fusion approaches namely minimum score, maximum score, simple sum, and user specific weighting. They have considered using user specific weighting because they found that some biometric traits cannot be reliably obtained from some people. Hence, they have given a lower weight to a fingerprint score and a higher weight to a finger-vein score to reduce the probability of a false

rejection. However, it appears that the weight assignment is rather on intuitive basis and not on any mathematical logic. As mentioned earlier, focus of the proposed work in this paper is mainly on enhancing accuracy of unimodal system so that it should be useful for HSA or very, very low FAR applications. Further, it may be observed that among various hand-based modalities, PP modality gives reasonably good accuracy. Therefore, focus of the proposed work is to explore the techniques, which may be useful for further improving the recognition accuracy of the PP modality based on logical, sound mathematical approach. The proposed unimodal system gives enhanced accuracy of 99.25% with very low FAR level of 0.0001 which is substantially greater than present day multimodal systems quoted above. Before explaining image capture, processing, and feature extraction, we introduce the mathematical basis for binary signal detection, with a view to understand the relationship between important parameters like GAR_{min}, ROC, accuracy, etc. in the following section.

3 Mathematical preliminaries

3.1 Mathematical background for binary signal detection

The problem of binary detection is formulated and analyzed in various signal detection and estimation books [24, 25]. The simplest binary communication system is shown in Fig. 1. A typical simple case consists of a single observation of the received signal corrupted by additive noise. The input signal is assumed to be in the binary form with two distinct values " m_0 " and " m_1 ," corresponding to two binary hypotheses, " H_0 " and " H_1 " respectively. The received signal "r" can be expressed as,

$$r/H_i = m/H_i + noise (i = 0 \text{ or } 1)$$
 (1)

In the above Eq. (1), symbol " r/H_i " represents received signal "r" assuming hypothesis " H_i " is true and symbol " m/H_i " represents mean value of the received signal assuming hypothesis " H_i " is true. The last term "noise"

represents undesirable degradations due to fine dust, illumination effects, blurring effects, etc. In this paper, it is further assumed that overall effect of all degradations due to central limit theorem of statistics leads to zero mean Gaussian distribution with variance " σ^2 ." Further, the probability density function (PDF) for the observed signal can be expressed as,

$$P(r/Hi) \boxtimes G(m_i, \sigma^2)$$
 (2)

In Eq. (2), symbol " " means equality in PDF and "G" represents standard Gaussian distribution. For the simplest example of binary hypothesis testing considered, the generalized likelihood ratio test (GLRT) has been derived as [24, 25],

$$GLRT = \frac{P(r|H_1)}{P(r|H_0)} \begin{array}{c} H_1 \\ > \\ < \\ H_0 \end{array}$$
 (3)

In Eq. (3), " γ " represents decision threshold. For the simple case of single observation, the above equation leads to,

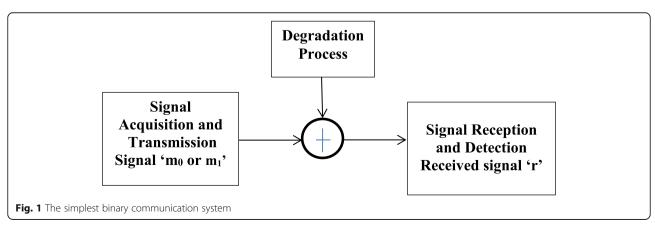
$$\begin{array}{c}
H_1 \\
r > \gamma \\
< Y \\
H_0
\end{array} \tag{4}$$

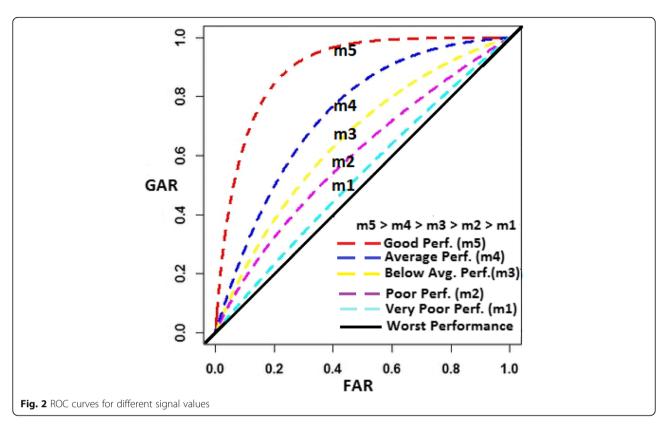
In Eq. (4), the term " γ " is given by Eq. (5).

$$\gamma = \frac{\sigma^2}{m_1} \ln(\eta) + \frac{m_1}{2} \tag{5}$$

In Eq. (3), signal value for the hypothesis " H_0 " has been assumed to be zero (i.e., $m_0 = 0$) for simplicity and in Eq. (5), " η " represents ratio of occurrence of a priori probabilities of two hypotheses H_0 and H_1 . For equiprobable hypotheses, " $\eta = 1$ " and decision threshold becomes " $\gamma = m_1/2$ " which is expected.

The GAR can now be expressed as,





$$GAR = \int_{\gamma}^{\infty} P(r|H_1) dr$$
 (6)

Similarly, FAR can be expressed as,

$$FAR = \int_{\gamma}^{\infty} P(r|H_0)dr \tag{7}$$

In biometric terms GAR and FAR are known as "True Positive" and "False Positive" respectively. The ROC curve represents plot of "GAR versus FAR" as value of decision threshold " γ " is varied from very low value to very large value. As " γ " threshold increases, both GAR and FAR get reduced. In this case, we follow the test suggested by Neyman-Pearson (NP) [24], in which decision threshold is pre decided by level of maximum FAR permissible in the application. In this method, GAR is maximized for the stipulated value of FAR. In high security applications, value of FAR \leq 0.0001 (maximum of one among 10,000 samples may be falsely acceptable). Hence, we set our threshold based on equation no. (7), with FAR = 0.0001.

Typical ROC characteristics for the simplest case are shown in the Fig. 2, where typical signal values, $m_5 > m_4 > m_3 > m_2 > m_1$ are used and " m_0 " is assumed to be zero. The ideal characteristics would be GAR = 1 and



Fig. 3 Data acquisition system

FAR = 0 and the worst scenario, GAR = FAR which is diagonal solid line marked as "Worst Performance" in Fig. 2. It is observed that as the signal value increases, the ROC curve shifts toward the ideal curve and the detection performance improves [24].

The error in the binary system can be defined as,

$$E_{\rm r} = [P_0 \times ({\rm false~acceptance~rate}) + P_1 \times ({\rm genuine~rejection~rate})]$$

(8)

(12)

In Eq. (8), genuine rejection rate (GRR) represents false negative for biometric system. Further, P_0 and P_1 represent a priori probabilities of hypotheses H_0 and H_1 respectively. Assuming two hypotheses to be equally likely, i.e., $P_0 = P_1 = \frac{1}{2}$, the error situation can be expressed as,

$$E_{\rm r} = (\rm FAR + \rm GRR)/2 \tag{9}$$

The detection accuracy can be expressed as,

$$Accuracy = (1-Er) \tag{10}$$

For the simple equiprobable binary hypothesis, Eq. (10) leads to,

$$Accuracy = \left(1 - \frac{(FAR + (1 - GAR))}{2}\right) \tag{11}$$

Further, for high security applications, where FAR is very small compared to GAR, above Eq. (11) approximates to,

Percentage accuracy
$$_{min.} = \begin{bmatrix} \frac{1}{2} \left(1 + \textit{GAR}_{min.}\right) \end{bmatrix} \times 100\%$$

It is readily seen from the ROC that GAR_{min} is the value of GAR, at which the ROC curves depart from FAR=0 (i.e., $\emph{Y}\text{-}axis$) tangentially. Further, as a value of AUC (0.5 < AUC < 1.0) increases, the value of GAR_{min} also increases, which leads to accuracy enhancement. For the worst scenario, $GAR_{min}=0$. For ideal scenario, GAR_{min} approaches to 1. Thus the accuracy level increases from 50 to 100%. One more commonly used method in binary recognition is equal error rate (EER) method, i.e., FAR=GRR. In this case, for equiprobable hypotheses, the accuracy in % units can be expressed as,

Percentage accuracy =
$$(1-GRR) \times 100$$
 (13)

Percentage accuracy =
$$(GAR) \times 100$$
 (14)

However, in this case, GAR has to be determined at the EER point. In this paper, as our main focus is on high security applications, we use only NP test explained above and evaluate the percentage accuracy using Eq. (12).

3.2 System effectiveness

The term "system effectiveness ϵ " represents the quantitative measure of effectiveness of biometric recognition system, which can be defined as follows,

System effectiveness (
$$\epsilon$$
) = $\left(\frac{\text{GAR}_{\text{min.}} \times t_{\text{max.}}}{t}\right) \times \textit{Cc}$ (15

In Eq. (15), " $t_{\rm max}$ " represents maximum permissible time as per system requirements stipulated and "t"

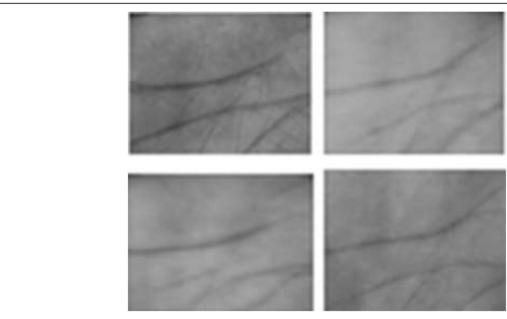


Fig. 4 Enhanced palm prints ROI images

represents actual time required for recognition process. Further, " C_C " represents the hardware complexity of the computer configuration used. Effectiveness of the system increases with increase in " GAR_{\min} " which enhances the recognition accuracy and with reduction in the actual recognition time t. The system effectiveness also increases with increase in complexity of the computer configuration used. The higher the value of system effectiveness, the better will be the biometric system.

With above analytical background and definitions, we now consider the image acquisition, feature extraction techniques, and features mapping techniques used for the biometric recognition system.

4 Image data acquisition, feature extractions, and feature mapping techniques

4.1 Image capture process

The data acquisition system (DAS) has been designed, developed, and fabricated. Regarding this DAS and the required image pre-processing, we have explained in detail in our paper published during the Conference on Advances in Signal Processing (CASP), 2016 [11]. DAS to extract PP modality is shown in Fig. 3. Webcam with medium resolution 640 × 480 has been used to acquire images and database of 150 users has been created. In this case, all 150 users were asked to wash/clean their hands before image capture process. This ensures that the database was reasonably error free data and only noise during capture can lead to the degradation of images. For every user, ten images of PP modality have been captured. Extraction of PP ROI has been discussed in detail in the paper published during International Conference on Electronics and Communication Systems (ICECS), 2014 [12]. The enhanced ROIs for palm print images are shown in Fig. 4. The biometric feature extraction is discussed in the following subsection.

4.2 Techniques for palm print feature extraction

Two techniques namely Harris Corner Detector (HCD) and DWT are used for feature extraction. These techniques are briefly discussed below:

4.2.1 Feature extraction using HCD

HCD algorithm was used to extract palm print feature vector [26]. Algorithm is stepwise explained in the following.

Step 1: Compute *X* and *Y* derivatives of image by convolving image "*I*" with Prewitt operator.

$$I_x = G_\sigma^x * I, I_\gamma = G_\sigma^y * I \tag{16}$$

In Eq. 16, G_{σ}^{x} = Prewitt vertical edge operator and G_{σ}^{y} = Prewitt horizontal edge operator

Step 2: Compute products of derivatives at every pixel.

$$I_{x}^{2} = I_{x}.I_{x}, I_{y}^{2} = I_{y}.I_{y}, I_{x}I_{y} = I_{x}.I_{y}$$
 (17)

Step 3: Compute the sums of the products of derivatives at each pixel.

$$I_{x2} = G_{\sigma'} * I_{x}^{2}, I_{y2} = G_{\sigma'} * I_{y}^{2}, I_{xy}$$

= $G_{\sigma'} * I_{x}I_{y}$ (18)

In Eq. (18), $G_{\sigma'}$ = Gaussian filter





0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	1	1	1	0	0
0	1	0	0	1	1	1	0
1	0	0	0	1	1	0	0
0	0	0	0	1	1	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

Fig. 5 Palm print with corners and its binary matrix

Step 4: Define at each pixel (x, y) the matrix.

$$M = \begin{bmatrix} I_{x2}(x,y) & I_{xy}(x,y) \\ I_{xy}(x,y) & I_{y2}(x,y) \end{bmatrix}$$
 (19)

Step 5: Compute the "response" of the detector at each pixel.

$$R = Det(M) - K(Trace(M))^{2}$$
 (20)

In Eq. (20), "K" is a constant, which lies in between the range 0.04 to 0.07 [12, 26]. All pixels that have scores greater than a certain threshold value "R" have been marked as the "Corner points or Tracking points" on the ROI of palm print image. We have taken the size of this ROI 256 by 256 pixels. Number of corner points lies in between 12 and 16 depending upon the value of "K" [12, 26]. These corner points have been mapped from ROI of 256 by 256 pixels into a binary matrix of size 8×8 , as shown in Fig. 5. Thus, PP feature vector has been created. HCD has few limitations. HCD consumes substantial time to detect the corners. Further, as HCD uses spatial domain processing, the accuracies may be adversely affected due to intensity artifacts, rotation effects, degradation effects, etc.

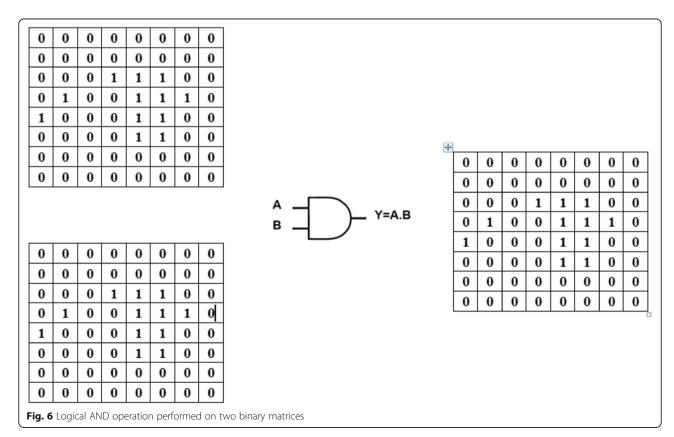
4.2.2 Palm print feature extraction using DWT

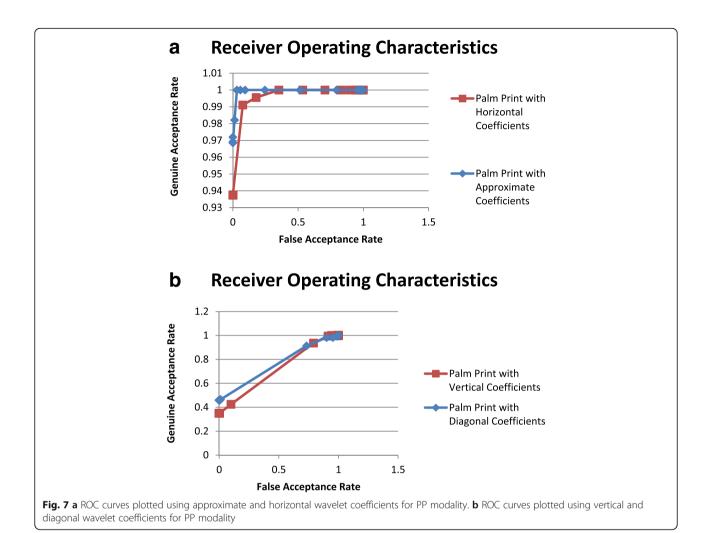
The methodology for extraction of DWT features has been explained in detail in Pallavi Deshpande et al. [11]. As indicated therein, two vectors of size 25×54 , one for the approximate coefficients and the other for horizontal coefficients for each of the image, are stored in the database. In this paper, a novel algorithm for optimally choosing the weights of the approximate and horizontal coefficients to create a final feature vector of the PP image is proposed to enhance the accuracy of the system. Further, empirical-based technique and optimal-based "optimum weights algorithm" are used to decide the weights of approximate and horizontal coefficients in the combined feature vectors to boost the accuracy.

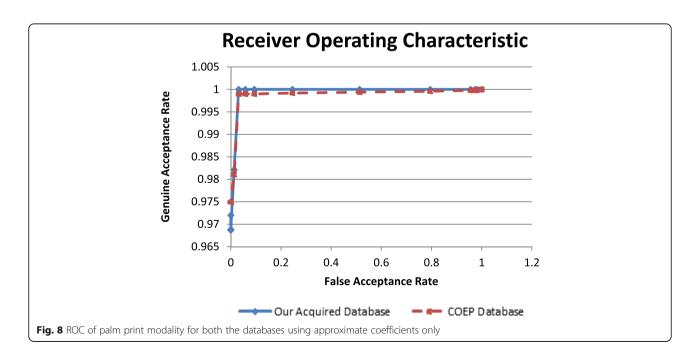
4.3 Feature matching

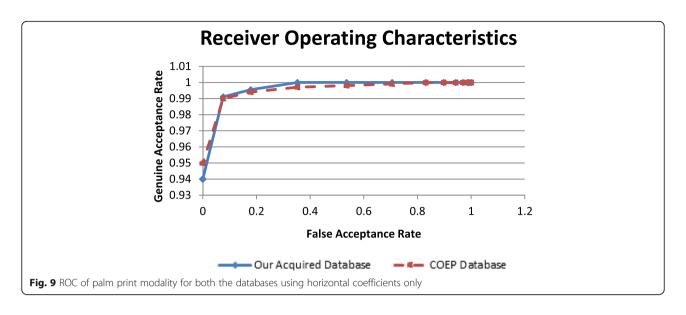
4.3.1 Methodology for mapping HCD features

Feature vector, i.e., binary matrix of new user (size 8 by 8), is compared with every stored feature matrix (each of size 8 by 8) in the training database. Logical "AND" operation between this new user's matrix is done with each and every feature vector/matrix present in the database. For genuine user, maximum number of 1's will be obtained through this logical ANDING operation in the output matrix. Finally, summation of all 1's in the output matrix will give the overall score. The maximum score gives best match as shown in Fig. 6 [12].









4.3.2 Methodology for mapping DWT features

In this case, the Euclidean distance (E.D.) is computed between the new user's DWT feature vector of size 25×54 and every stored DWT feature vector (of size 25×54) in the database using Eq. (21),

E.D. =
$$\sqrt{\sum_{i=1}^{L} (x_i - y_i)^2}$$
 (21)

In this case, " x_1 , x_2 x_n " represent coefficients from feature vector of new user and " y_1 , y_2 ... y_n " represent coefficients from feature vector of stored palm print and "L" represents size of feature vector which is of size 25×54 . The minimum Euclidean distance gives the best match.

4.4 Methodology for accuracy prediction

Different techniques are used to create feature vectors for the proposed PP based biometric system. Their accuracy estimation methods are given below.

4.4.1 HCD technique-based biometric recognition system

For the HCD features, considering the correct assessment of GAR using the acquired database, GAR_{min} has been estimated as 0.9536. This is based on the entire mapping process carried out within the database, where

out of 220 images, the exact match was found for 210 images. For rest of the ten images, there was mismatch, thus giving ${\rm GAR_{min.}}$ 0.9536. Based on this, accuracy for high security applications works out to 97.68% using Eq. (12). Even though the above accuracy appears to be good, due to need for pixel by pixel mapping and totally spatial domain signal processing, as mentioned earlier, the HCD would be more likely to degrade the accuracy performance further. The DWT, on the other hand, has some distinct advantages.

DWT technique uses joint time-frequency domain approach, hence pixel by pixel comparison is not required. Further, the degradations due to rotation, size, and brightness effects are much less severe for DWT [13, 27]. Typical ROC curves for PP modality using DWT technique are plotted for acquired error free database of 150 users and are shown in Fig. 7a, b. All four types of DWT coefficients (i.e., approximate, horizontal, vertical, and diagonal) are extracted and ROCs are plotted for all four types of DWT coefficients. After comparing ROC characteristics of all four types of DWT coefficients, it can be readily seen that a ROC for approximate coefficients is very close to the ideal ROC curve (AUC lies in between 0.95 and 1.0). ROCs for vertical and diagonal coefficients are far away from the ideal curve (in fact they are nearer to the worst scenario, i.e., AUC equals to 0.50). The ROC curve for horizontal coefficient lies in

Table 1 Comparison using three feature extraction techniques

Sr.	Method used	Acquired datab	pase	COEP database		
No.		GAR _{min}	Accuracy	GAR _{min}	Accuracy	
1	Harris Corner Detector	0.9536	97.68%	=	=	
2	DWT with approximate coefficients	0.972	98.60%	0.975	98.75%	
3	DWT with horizontal coefficients	0.940	97.00%	0.950	97.50%	

between the two extremes. Therefore, it is proposed to use "only approximate coefficients" or "only horizontal coefficients" or "the combination of approximate plus horizontal coefficients" for the formation of the feature vectors. Analysis and further enhancing accuracy using approximate and horizontal DWT coefficients is discussed in the following subsection.

4.4.2 Feature vectors using "only approximate" DWT coefficients-based biometric recognition system

Using feature vectors based on only approximate DWT coefficients, as per methodology discussed in Section 4.2.2, ROCs for our acquired PP database of 150 users and the standard PP database provided by College of Engineering, Pune (COEP) are shown in Fig. 8. As explained earlier, tangential departure of the ROC from FAR = 0 (i.e., Y-axis) gives the values for GAR_{min} and AUC values.

Following performance level can be determined using the ROC curve plotted for our own acquired database.

- $AUC_{APP} = 0.975$
- $GAR_{min} = 0.972$
- Accuracy_{min} = 98.60% using Eq. (12)

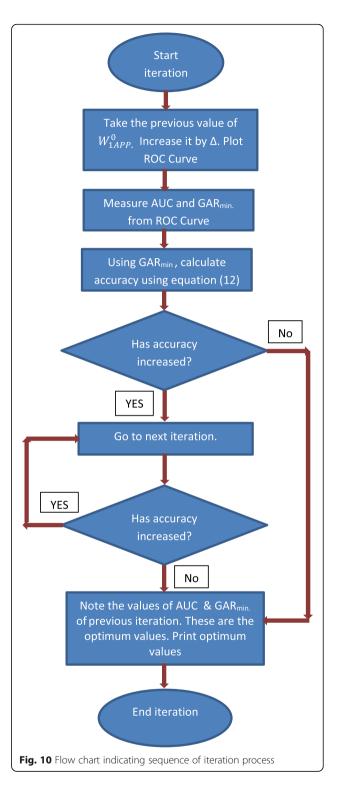
For benchmarking purposes, the standard publically available COEP database is used. (http://www.coep. org.in/resources/coeppalmprintdatabase). This database consists of eight different images of single user having resolution of 1600×1200 pixels per image. The database consists of total 1344 images pertaining to 168 users. Figure 8 also includes ROC of the palm print modality using COEP database. Following performance level can be determined using the ROC curve.

- AUC_{APP} = 0.98
- $GAR_{min} = 0.975$
- Accuracy_{min} = 98.75%

4.4.3 Feature vectors using "only horizontal" DWT coefficients-based biometric recognition system

Using identical approach as explained in Section 4.2.2 ROCs are plotted using only horizontal DWT coefficients. The ROC curves for both the databases are shown in Fig. 9. The parameters namely AUC_{HPP} and GAR_{min} are determined and accuracy is calculated using Eq. (12) for acquired database as shown below.

- AUC_{HPP} = 0.9211
- GAR_{min} = 0.94
- Accuracy_{min} = 97.00%



Similarly, Fig. 9 also includes ROC of the palm print modality for COEP database. Following performance level is determined using the ROC curve.

- AUC_{HPP} = 0.94
- $GAR_{min} = 0.95$

Table 2 Summary of parameters at different iterations for our acquired database

Sr. No. of iteration (i)	W ⁱ _{1APP}	W ⁱ _{2HPP}	GAR _{min}	% of minimum accuracy achievable	Performance
0	0.513227513	0.486772487	0.9800	99.00	Good
1	0.563227513	0.438172487	0.9810	99.05	Good
2	0.613227513	0.389572487	0.9810	99.05	Good
3	0.663227513	0.340822487	0.9810	99.05	Good
4	0.713227513	0.292072487	0.9820	99.10	Better
5	0.763227513	0.243247487	0.9820	99.10	Better
6	0.813227513	0.191322487	0.985	99.25	Best
7	0.863227513	0.144422487	0.9820	99.10	Better
8	0.913227513	0.09522386	0.9810	99.05	Good

• Accuracy_{min} = 97.50%

Table 1 shows GAR_{min} and accuracy values using three feature extraction techniques for PP recognition. Comparing the accuracies for DWT features for our database and COEP standard database, it is seen that our algorithm gives comparable performance levels for both databases. This indicates that the algorithm proposed can very well be used irrespective of database. As accuracies predicted for our own database (which is error free database) and COEP database are almost same, it also suggests that COEP database is also fairly clean and error free database.

The accuracies indicated in Table 1 are good. However, in order to further boost accuracies, "Empirical method" or "OWA" can be used. These methods are discussed in the following subsections.

4.5 Performance prediction using combination of feature vectors

Two different methods namely "OWA" and "Empirical method" are discussed below to combine approximate and horizontal DWT coefficients to create new feature vectors in order to boost accuracy of the system.

4.5.1 Performance prediction using analytical approach

Suppose there are "n" coefficients be combined, the generalized formulation to decide the weights of coefficients of the system can be expressed as

$$W_n = \alpha \times AUC_n \text{ with, } \sum_{n=1}^N W_n = 1$$
 (22)

In Eq. (22), each of $W_{\rm n}$ (0 < $W_{\rm n} \le$ 1) represents weight for the nth coefficient with AUC for ROC curve denoted by AUC_n (0.5 < AUC_n \le 1). In our case, we consider only two coefficients, approximate and horizontal. Therefore, N=2. For deciding optimum values of weights $W_{\rm 1APP}$ and $W_{\rm 2HPP}$ areas under two ROCs of acquired database (shown in Figs. 7 and 8 respectively) are to be considered.

The proportionality constant " α " can now be determined using

$$W_{1\text{APP}} + W_{2\text{HPP}} = 1 \tag{23}$$

Above Eq. (23) leads to the equation,

$$W_n = \frac{AUC_n}{\sum_{i=1}^{N} AUC_n} \tag{24}$$

In the proposed system, considering AUC_{APP} = 0.975, AUC_{HPP} = 0.9211, we get $\alpha = 0.5291005291$, giving values of $W_{1App}^0 = 0.5132275132$ and $W_{2HPP}^0 = 0.4867724868$.

We now commence our iteration process for the zeroth iteration (i=0) with above values of W^0_{1APP} and W^0_{2HPP} By using these weights, area under the revised ROC curve (AUC⁰) was 0.9720 and GAR_{min} was measured as 0.9800. This results in accuracy of 99.00% using Eq. (12). The performance can be further improved through series of iterations as illustrated below.

For this, it was observed that $AUC_{APP} > AUC_{HPP}$. Therefore, we go on increasing weight of approximate coefficients " W_{1APP}^0 " in small positive steps ($\Delta = 0.05$) in each iteration and weight of horizontal coefficients " W_{2HPP}^0 " has to be decreased appropriately.

The general equations for iterations are as follows.

$$W_{1APP}^{i+1} = W_{1APP}^{i} + \Delta \tag{25}$$

and

Table 3 Results obtained for different combinations of weights

Sr. No.	E _{SUMPP}	Our acquired database				
		GAR _{min}	Accuracy	Performance		
1	$[(0.5 \times E_{APP}) + (0.5 \times E_{HPP})]$	0.9810	99.05	Good		
2	$[(0.6 \times E_{APP}) + (0.4 \times E_{HPP})]$	0.9810	99.05	Good		
3	$[(0.7 \times E_{APP}) + (0.3 \times E_{HPP})]$	0.9820	99.10	Better		
4	$[(0.8 \times E_{APP}) + (0.2 \times E_{HPP})]$	0.984	99.20	Best		
5	$[(0.85 \times E_{APP}) + (0.15 \times E_{HPP})]$	0.9810	99.05	Good		

Table 4 Comparison between two configurations

Sr. No.	Parameters	Configuration 1 Dell Inspiron N5050	Configuration 2 HP Pavilion 15 cc134tx
1	Processor used	Intel I ₃ 2350M	Intel Core i7
2	Clock speed	2.3 GHz	4.0 GHz
3	Processor generation	2nd generation	8th generation

$$W^{i+1}_{2HPP} = W^{i}_{2HPP} - \Delta \times AUC^{i}$$
 (26) $W^{2}_{1APP} = 0.613227513 \text{ and } W^{2}_{2HPP} = 0.389572487$

In Eqs. (25) and (26), W^{i+1} represents the weight assigned for (i+1) iteration, where i=1, 2, 3, 4... represents the iteration sequence number and AUC^i represents area under the corresponding ROC curve after ith iteration. After each iteration, two parameters namely AUC and the new value of GAR_{min} with revised ROC are determined. Using the GARmin, the accuracy prediction is done using Eq. (12). It is observed that after every iteration, the accuracy goes on increasing. Iteration process is continued until accuracy reaches to maximum. After this, any further increase in $W_{1\text{APP}}$ leads to reduced value of GAR_{min} which decreases the accuracy. We stop the iteration process at this point. Typical sequence of iterations is depicted in Fig. 10. The iteration process implemented is illustrated in the following.

4.5.1.1 First iteration Let us take i=1. Take the previous value of $W_{1\text{APP}}^0 = 0.5132275132$ and $\Delta = 0.05$. Using Eq. (25), we get $W_{1\text{APP}}^1 = \text{equal}$ to 0.563227513. Using Eq. (26), we get $W_{2\text{HPP}}^1 = \text{equal}$ to 0.438172487. Using these new weights, the new revised ROC was plotted and the area under this new ROC curve (AUC¹) was 0.9720 and GAR_{min} was measured as 0.9810, giving an accuracy of 99.05%. To improve the accuracy further, we continued the same process in second iteration.

4.5.1.2 Second iteration To explore further improvement possible, the weight for approximate coefficients was further increased by $\Delta = 0.05$ to $W^2_{\rm 1APP} = 0.61322$ 7513 . Following exactly identical procedure, as in the first iteration, the new weights are determined as,

Using these new weights, the new ROC was plotted and the area under this new ROC curve (AUC^2) was 0.9750 and GAR_{min} was measured as 0.9820, giving an accuracy of 99.10% which is marginally higher than the accuracy obtained in the first iteration. This process has been continued further. Table 2 shows the summary of the number of iterations carried out.

From Table 2, it can be observed that values of weights for the 6th iteration yields the highest maximum accuracy. Beyond this, the accuracy decreases for the subsequent iterations. Hence, those values of weights are considered as optimal values. Hence, the optimum values of the weights after 6th iteration are as follows, $W^6_{1APP} = 0.813227513$ and $W^6_{2HPP} = 0.191322487$.

Using these new weights, the new ROC was plotted and the area under this new ROC curve was 0.9776 and GAR_{min} works out to be 0.9885, giving an accuracy of 99.25%, which is the highest possible value of the accuracy of the system. Based on the above optimum weight algorithm, Sum rule is,

$$E_{SUM} = (0.813227513 \times W_{APP}) + (0.191322487 \times W_{HPP})$$
(27)

4.5.2 Weights selection using empirical method

In addition to analytical method, one can use simple empirical method to decide the weights. The simple method is described in the following. After feature extraction, score normalization is done using "Z score" normalization technique [4]. In order to increase the accuracy of the system, the horizontal and approximate normalized scores are combined with the following summing rule:

Table 5 Mapping time required using approximate plus horizontal coefficients

Sr.	Acquired database	Mapping time required per ima	Mapping time required per image in seconds			
No.	(approximate + horizontal coefficients)	Configuration 1 Dell Inspiron N5050	Configuration 2 HP Pavilion 15 cc134tx			
1	60 users $(60 \times 6 = 360 \text{ hands})$	1.88625	0.96312			
2	100 users $(100 \times 6 = 600 \text{ hands})$	2.99375	1.49687			
3	150 users $(150 \times 6 = 900 \text{ hands})$	4.115625	2.15781			

Table 6 Mapping time required using only approximate coefficients

Sr. No.	Acquired database	Mapping time required per ima	Mapping time required per image in seconds			
	(approximate coefficients)	Configuration 1 Dell Inspiron N5050	Configuration 2 HP Pavilion 15 cc134tx			
1	60 users $(60 \times 6 = 360 \text{ hands})$	1.77797	0.88998			
2	100 users $(100 \times 6 = 600 \text{ hands})$	2.96562	1.48281			
3	150 users $(150 \times 6 = 900 \text{ hands})$	3.948437	1.995618			

$$E_{SUM} = [(W_{1APP} \times NS_{APP}) + (W_{2HPP} \times NS_{HPP})]$$
(28)

In Eq. 28, $W_{1\mathrm{APP}}$ and $W_{2\mathrm{HPP}}$ are the weights empirically chosen for normalized scores of approximate (NS_{APP}) and horizontal (NS_{HPP}) coefficients of PP modality respectively. Here, we start with equal weights $W_{1\mathrm{APP}} = W_{2\mathrm{HPP}} = 0.5$. Comparing the two ROC curves, we know that $\mathrm{AUC}_{\mathrm{APP}} > \mathrm{AUC}_{\mathrm{HPP}}$. Therefore, weight of approximate coefficients is increased in the step of 0.1 and weight of horizontal coefficients is decreased accordingly. For each step, the new ROC is plotted and $\mathrm{GAR}_{\mathrm{min}}$ is determined. The accuracy is determined using Eq. 12. The results of $\mathrm{GAR}_{\mathrm{min}}$ and accuracy for different empirical choices of $W_{1\mathrm{APP}}$ and $W_{2\mathrm{HPP}}$ are indicated in Table 3.

From Table 3, it can be observed that GAR_{min} and accuracy values appear to be best for the following rule:

$$E_{SUM} = [(0.8 \times NS_{APP}) + (0.2 \times NS_{HPP})]$$
 (29)

It is readily observed that the above weights based on empirical method are fairly closer to the weights suggested by "OWA" in Section 4.5.1.

4.6 Evaluation of the system effectiveness

Time required for extracting palm print features of a new users' hand image is observed to be approximately 3 se. After feature extraction, the average feature mapping time has also been recorded. While taking average, 20 iterations are done and average time of these twenty iterations is recorded. The average mapping time varies according to database size (i.e., 60, 100 or 150 users) and also depends upon the computational complexity in the hardware used. Comparison between the two configurations from hardware complexity view point is depicted in Table 4 below.

All the other parameters such as type of display, Cache memory, RAM/ROM sizes, etc. are not relevant for our application and therefore not considered for complexity estimation. Here, clock speeds for the two configurations are different. Cost for the two configurations would vary substantially and it would also depend upon local taxes, duties, etc. Therefore, the cost is not included in deciding Cc values. We determine the computational complexity "Cc" factor as follows:

Cc for configuration 1 = Dell Inspiron N5050 = 1.0
Cc for configuration 2 = HP Pavilion 15 cc134tx
=
$$4GHz/2.2GHz = 1.8181$$

Tables 5 and 6 show the mapping time required for the two main feature extraction techniques namely, only approximate DWT coefficients and combined approximate plus horizontal DWT coefficients using above configurations. These two configurations were used for system effectiveness calculations as the two configurations were readily available with us at our research center. Form Tables 5 and 6, it is seen that there is very small difference between mapping times for DWT methods using "only approximate coefficients" and using combined "approximate plus horizontal coefficients" for two different configurations. But the accuracy prediction results indicate that there is some definite improvement in accuracy when both "approximate and horizontal coefficients" are combined (refer serial no. 6 from Table no. 2).

It can be seen from Tables 5 and 6 that mapping time varies as per size of database. As expected, the mapping time increases if size of the database is increased from 60 to 100 and from 100 to 150. Therefore, system effectiveness calculations will also change as per the size of the database. Just for illustration, a system effectiveness

Table 7 Summary of results for $C_C = 1.0$

	Table 7 Sammary of results for El 1.0						
Sr.	Technique used	GAR _{min}	t in seconds	System effectiveness			
No.			$C_C = 1.0$	for $C_C = 1.0$			
1	DWT with approximate coefficients	0.972	2.96562	1.6387804			
2	DWT with horizontal coefficients	0.940	2.96560	1.5848394			
3	DWT with approximate and horizontal coefficients	0.985	2.99375	1.6450939			

Table 8 Summary of results for $C_C = 1.8181$

Sr.	Technique used	GAR _{min}	t in seconds	System effectiveness for $C_C = 1.8181$	
No.			$C_C = 1.8181$		
1	DWT with approximate coefficients	0.972	1.48281	5.9589	
2	DWT with horizontal coefficients	0.940	1.44232	5.9245	
3	DWT with approximate and horizontal coefficients	0.985	1.496875	5.9818	

calculation for the database of 100 users is shown in the next section.

5 Results and discussion

Based on the approach described in Section 4 above, the summarized results are presented in what follows. Further illustrative results for database of 100 users only are included.

5.1 System effectiveness calculations for N = 100

Tables 7 and 8 summarize the results for system effectiveness for database of 100 users for the two configurations $C_C = 1.0$ and $C_C = 1.8181$ respectively. As discussed in Subsection 3.2, we use Eq. (15) for system effectiveness calculations.

It is clearly seen from Table 8 that when the "configuration 2" computing facility is used for combined "approximate and horizontal coefficients" technique with the use of weight optimization algorithm, the effectiveness increases to 5.9818. This is due to substantial higher clock frequency of configuration 2, as compared to configuration 1.

5.2 Performance prediction using combination of feature vectors-based biometric recognition system

Figure 11 shows ROC of the palm print modality using both approximate and horizontal coefficients as per "optimal weights algorithm."

- $AUC_{PP} = 0.9776$
- $GAR_{min} = 0.985$
- Accuracy_{min} = 99.25%

Similar procedure was also carried out for COEP database for validation and benching marking of the optimal weights algorithm. Figure 11 also shows ROC of the palm print modality using both approximate and horizontal coefficients using optimum weights algorithm.

- AUC_{PP} = 0.97
- $GAR_{min} = 0.984$
- Accuracy_{min} = 99.20%

System gives an enhanced accuracy of 99.25% using this "optimal weights algorithm." From the above discussions, it can be seen that ROC and accuracy of PP modality using combined approximate and horizontal

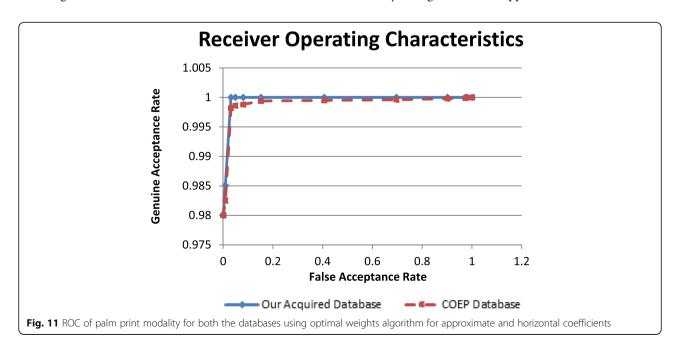


Table 9 Comparison of detection parameters among different methods

Sr.	Method used		Acquired database		COEP database	
No.		GAR _{min}	Accuracy	GAR _{min}	Accuracy	
1	Harris Corner Detector	0.9536	97.68%	=	=	
2	Horizontal DWT coefficients only	0.940	97.00%	0.950	97.50%	
3	Approximate DWT coefficients only	0.972	98.60%	0.975	98.75%	
4	Combined approximate plus horizontal DWT coefficients using optimum weights algorithm.	0.985	99.25%	0.984	99.20%	

coefficients are certainly better than ROC and accuracy of palm print modality using only approximate coefficients or using only horizontal coefficients. The summarized results using different techniques using our own database and also using a publically available COEP database are depicted in Table 9. It may be seen from Table 9 that our proposed "optimum weights algorithm" gives same enhanced accuracies using acquired database as well as COEP database. Further, we make use of only two techniques indicated at serial no.3 and serial no.4 (refer to Table 9) as they provide best possible accuracies. It is proposed to use optimum weight algorithm with values of 0.81 for the approximate coefficients and 0.19 for horizontal coefficients, as it would provide best possible percentage accuracy.

6 Conclusion and future scope

The paper provides a mathematical basis for evaluating the accuracy of the biometric recognition system. This paper clearly brings out a strong correlation between the detection accuracy of the system with the area under the curve (AUC) of its ROC. It has been shown that combining various useful DWT features leads to enhancement in accuracy. Use of iterative optimal weights algorithm (OWA) is proposed to further improve the accuracy of the system. Testing, validation, and benchmarking of the algorithm are done using the acquired database, as well as with standard publically available COEP database. The proposed system gives enhanced accuracy of 99.25% with very low FAR level of 0.0001. This represents fairly accurate and significantly user-friendly biometric system, suitable for higher security applications. Even though we have used the algorithm only for combining the two types of coefficients, the proposed optimization algorithm may be very effectively used for combining different normalized scores of any multimodal (N > 2) biometric recognition system, with a view to boost the accuracy and increase the effectiveness of multimodal systems. Further, one can also consider systematically extending the procedure to more number of modalities using the standard principles of mathematical induction.

Abbreviations

AUC: Area under the curve; DHV: Dorsal hand vein; DWT: Discrete wavelet transform; FAR: False acceptance rate; GAR: Genuine acceptance rate;

 ${\sf GAR}_{\sf min}$: Minimum value of genuine acceptance rate; HSA: High security applications; OWA: Optimal weights algorithm; PP: Palm print; PPP: Palm-phalanges print; ROC: Receiver operating characteristics

Symbols

 \in : System effectiveness; H: Ratio of occurrence of a priori probabilities of two hypotheses H0 and H1; $\stackrel{\text{\tiny \psi}}{=}$: Equality in PDF; Γ : Decision threshold

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Authors' contributions

All three authors made substantial contributions to conception and design, or acquisition of data, or analysis and interpretation of data. They have been involved in drafting the manuscript or revising it critically for important intellectual content. They have given final approval of the version to be published. Each author has participated sufficiently in the work to take public responsibility, for appropriate portions of the content and agreed to be accountable for all aspects of the work, in ensuring that questions related to the accuracy or integrity of any part of the work are appropriately investigated and resolved.

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Competing interests

The authors declare that they have no competing interests.

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