

Research Article

An Efficient Objective Intelligibility Measure for Frequency Domain Scramblers

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An objective performance measure is proposed to evaluate the intelligibility of a speech signal having its frequency subbands permuted. The proposed tool can be used to generate efficient keys for frequency domain scramblers as well as to assess the results of cryptanalysis.

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1. INTRODUCTION

The main goal of a scrambler is to make a speech signal unintelligible via the permutation of its frequency subbands. In this work, we assume a sampling frequency of 8 kHz and a filter bank with 8 channels, each using a filter with 128 coefficients. With N being the number of (permutable) subbands, there are $N!$ possible permutations. However, not all of them are efficient [1]; this is due to the fact that some of them result in a signal with high residual intelligibility. Objective measures in the technical literature, such as spectral distortion and segmental signal-to-noise ratio [2], are not appropriated for the task of evaluating intelligibility in scrambled speech; this is so because the objective is not the difference in spectra but how intelligible the signal is. In [3], a scheme for obtaining scores was proposed. This scheme (Beker score) took into account subbands shift, number of subbands kept in their original positions, continuity of the subbands, and occurrence (or not) of subband inversion (not taken into consideration here due to the structure of our frequency scrambler). From our experiments, we noted that even with a close to perfect continuity as in permutation $[5\ 6\ 7\ 8\ 1\ 2\ 3\ 4]^T$, the listener could not understand the signal. Therefore, the objective measure proposed herein does not take into account the continuity of subbands; instead, it introduces a subband

weighing as each subband has its own degree of importance, mainly determined by the presence of formants [4].

2. POSITION DISTANCE

By means of subjective tests, it was observed (for our 8-subband scrambler) that if all subbands are shifted in two or more positions, the scrambled signal becomes completely unintelligible for a nonexpert listener. Nevertheless, if the shift is of only one position, the signal is partially intelligible. In order to set a weight to the shift of one position, two phrases were scrambled with permutation $[2\ 1\ 4\ 3\ 6\ 5\ 8\ 7]^T$ and 14 (nonexpert) people listened four times each. A training session was carried out before the real one. A score was computed as the rate of the number of words correctly written and as the total number of words in the two phrases (including articles and prepositions). The average score was 35%. The following weights were then adopted: 1 for unshifted subbands, 0.35 for subbands shifted by one position, and 0 for subbands shifted by two or more positions.

3. SUBBAND WEIGHTS

Also employing subjective tests, it seemed that subbands containing the first three formants in their correct positions

guarantee 100% of intelligibility in spite of all other subbands being permuted. This fact suggests that an objective measure could be determined based exclusively on the position of these three subbands containing the first three formants. However, this measure would require formant extraction and therefore the measure would be signal-dependent, which should be avoided. In order to weigh each subband without signal dependence, we have extracted, using linear predictive code (LPC) parameters, the first three formants of a set of 10 phonetically based Portuguese spoken phrases. Each phrase was spoken by 20 different speakers, totalizing 200 phrases. The silence intervals were manually removed. The histograms of the first, the second, and the third formants were computed. It is known [4] that the first formant is the most important one for voiced speech and the third formant is the most important (among the 3 first ones) for unvoiced speech. Conversely, the second formant has approximately the same importance for both voiced and unvoiced speeches. According to our investigation, for short-time frames (around 8 milliseconds) from Portuguese, language spoken in Brazil, approximately 75% of the frames are voiced speech and 25% are unvoiced. Taking this information into account, we propose the following expression to weigh the i th subband:

$$SBW_i = \frac{(0.75M1_i + 0.5M2_i + 0.25M3_i)}{1.5}, \quad i = 1, \dots, N, \quad (1)$$

where $M1_i$, $M2_i$, and $M3_i$ are the percentages of the occurrence of the first, second, and third formants in the i th subband (to be obtained from the histograms).

In (1), the value 0.75 multiplying $M1_i$ is due to the fact that the first formant is the most important one for voiced frames, which represent 75% of all frames. Similarly, the value 0.25 multiplying $M3_i$ is due to the third formant being the most important one for unvoiced frames, which represent 25% of frames. Since the second formant has approximately the same importance for all frames, the constant multiplying $M2_i$ was set to 0.5, the mean of the previous values. The division by the normalization factor 1.5 was carried out in order to have the values of SBW_i between 0 and 1.

Table 1 shows the results of each subband weight computed from (1) with the percentages of occurrence of the first three formants at each subband (obtained from the procedure previously described) for all subbands from 1 to $N = 8$. It can be noted from this table that $\sum_{i=1}^N SBW_i = 1$. The next section proposes the new objective measure of intelligibility that takes into account the subband weight and the position distance.

4. COMPUTING THE OBJECTIVE MEASURE

With the results obtained in the two previous sections, we can formulate an expression for an objective performance measure (OM) based on what follows. (a) The intelligibility is a function of the shifts in the subbands of the three first formants. (b) The weights in Table 1 can be understood as the probability of one of the formants to belong to subband

i , that is, the importance (weight) of the subbands. (c) By shifting the “ x ” positions of one subband and multiplying the subband by the weight assigned to that position distance (1 if $x = 0$, 0.35 if $x = 1$, or 0 if $x > 1$), we are giving the due importance to the shifted subband. In order to better explain this new objective measure, we provide the following example.

Assume that we have permutation $POS2 = [1 \ 3 \ 2 \ 5 \ 4 \ 7 \ 6 \ 8]^T$ instead of the original sequence (clear signal) $POS1 = [1 \ 2 \ 3 \ 4 \ 5 \ 6 \ 7 \ 8]^T$. The following steps are used to describe how to compute the objective measure (OM) for this permutation.

- (1) Determine the position distance (PD) as the difference between $POS1$ and $POS2$, in absolute values. In this example, $PD = [0 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 0]^T$.
- (2) Determine the weight vector associated to this position difference (PDW). In this example, $PDW = [1 \ 0.35 \ 0.35 \ 0.35 \ 0.35 \ 0.35 \ 0.35 \ 1]^T$.
- (3) Form the subband weight (SBW) from Table 1 according to vector $POS2$, that is, $SBW = [33.74 \ 12.50 \ 15.36 \ 9.48 \ 9.40 \ 2.61 \ 12.66 \ 4.25]^T/100$.
- (4) Compute the OM from (2)

$$OM = \frac{(PDW^T SBW)}{MV}, \quad (2)$$

where the denominator is the maximum possible value for the numerator and is given by $MV = [1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1] SBW$. For this example, we have $MV = 1$ and $OM = 59.7\%$.

In the case of 8 permutable subbands, we have $8! = 40320$ different keys. For all possible keys, Figures 1(a) and 1(c) depict the histograms (number of outcomes per range of OM values) of the proposed objective measure and the Beker score [3]. (The Beker score, as implemented in [3], comprises a distance measure instead of an intelligibility measure; we have then mapped the score results such that mapped score = 32-score.) Meanwhile, Figures 1(b) and 1(d), having cumulative functions (similar to estimates of the cumulative probability distribution functions if divided by $8!$), show the number of keys for which the objective measure and the Beker score, respectively, are lower than a prescribed value. Note that the histograms from Figures 1(a) and 1(c) suggest that the probability density function of the OM is a superposition of its two effects: one due to the position distance (as in the pdf of the Beker score) and one due to the subband weight (only present in the OM). Based on Figure 1(b), if we assume, for instance, that 10 is the maximum value of the objective measure such that the signal is considered to be unintelligible (i.e., the corresponding key is efficient), then only approximately 13 000 out of the $8!$ can be used. This result reinforces the information in [1] which states that from the whole set of possible permutations, only a small set of keys can be considered efficient. If the same procedure is carried out employing the Beker score, the result would be around 10 000. We claim from this result that a slightly larger number of keys can be chosen when compared to the number obtained from the technique in [3]. The grounds for this claim come from the next section where we address the correlation of both objective measures with subjective tests.

TABLE 1: Subband weights.

Subband i	1	2	3	4	5	6	7	8
SBW $_i$	0.3374	0.1536	0.1250	0.0940	0.0948	0.1266	0.0261	0.0425

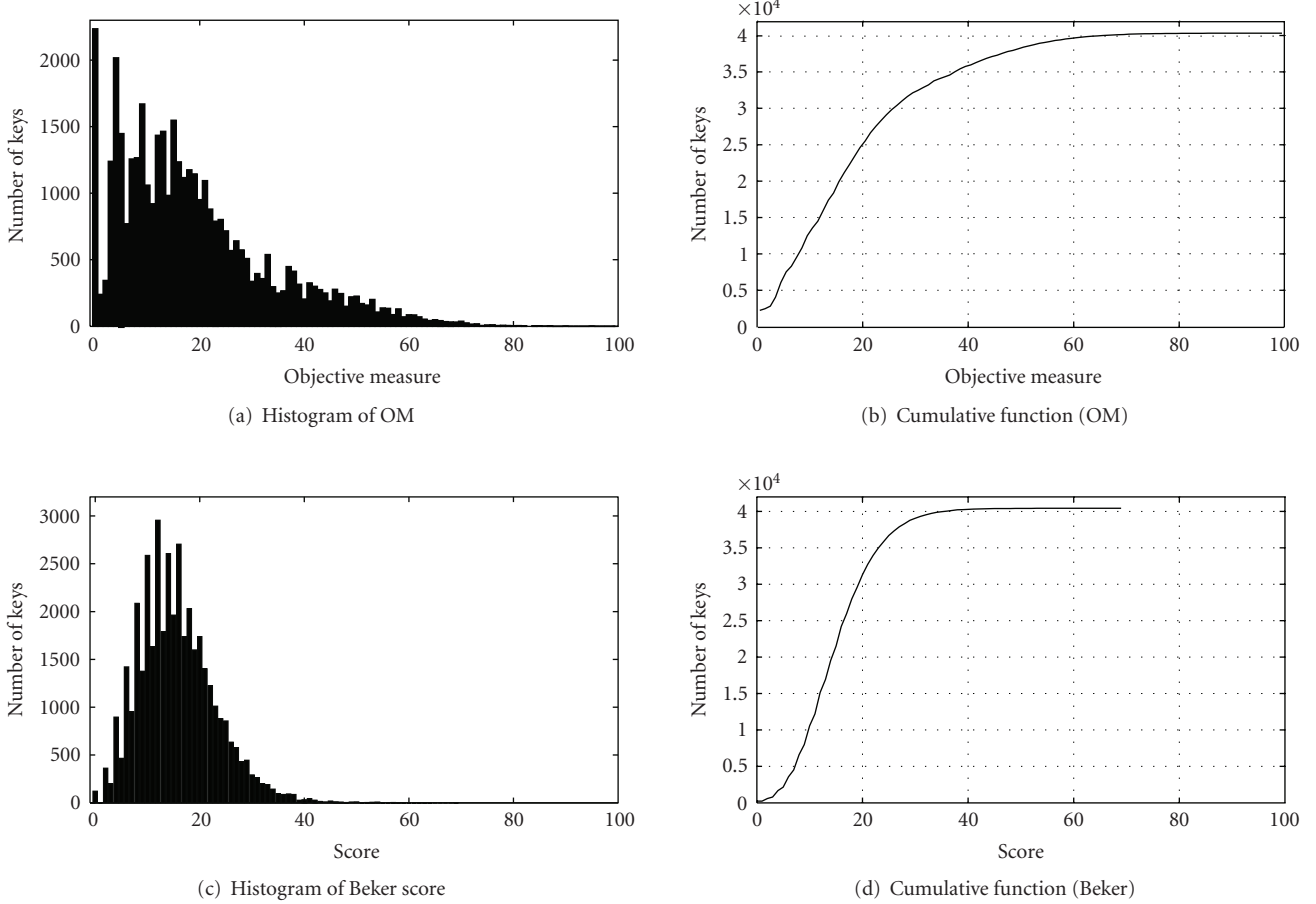


FIGURE 1: Histograms and cumulative functions of the OM and the Beker score.

5. EVALUATING THE CORRELATION WITH SUBJECTIVE TEST

In order to evaluate the correlation between the proposed objective measure and a subjective measure, an experiment was carried out as follows. Eight phrases from a set of phonetically balanced Brazilian-Portuguese phrases were selected. From subbands 1 to 8, the initial (clear speech) vector is given by $POS1 = [1\ 2\ 3\ 4\ 5\ 6\ 7\ 8]^T$. For this experiment, 8 permutations were chosen (each corresponding to a vector $POS2$ as in the previous section): $P1 = [8\ 7\ 3\ 4\ 5\ 6\ 1\ 2]^T$, $P2 = [2\ 1\ 4\ 3\ 6\ 5\ 8\ 7]^T$, $P3 = [1\ 3\ 2\ 5\ 4\ 7\ 6\ 8]^T$, $P4 = [3\ 2\ 1\ 4\ 7\ 6\ 5\ 8]^T$, $P5 = [1\ 2\ 8\ 7\ 6\ 5\ 4\ 3]^T$, $P6 = [3\ 4\ 1\ 2\ 5\ 6\ 7\ 8]^T$, $P7 = [2\ 1\ 3\ 4\ 5\ 6\ 7\ 8]^T$, and $P8 = [1\ 4\ 3\ 2\ 5\ 8\ 7\ 6]^T$. Using the same procedure previously described, the OM is computed for each of the 8 permutations. Each phrase was ciphered with a fixed key corresponding to the 8 permutations from P1 to P8, and 14 nonexperts listened 4 times to each phrase. For each of the 8 permutations, a subjective score was computed (SM from subjective measure) as the rate between the number of cor-

rect words and the total number of words. Table 2 shows both measures (OM and SM) and the absolute error ($|OM-SM|$) for the 8 permutations. From Table 2, the mean absolute error is computed and the result is 8.61%; this shows a good correlation between OM and SM. Another form of assessing the correlation is given by the so-called Spearman coefficient [3] which is widely used in nonparametric (ranking) correlation and is considered insensitive to outliers. In obtaining the Spearman coefficient, the permutations used in the experiment were ranked (from the largest to the smallest value of the OM, the SM, and the Beker score).

Table 3 presents the resulting rankings (the subjective measure rankings were ordered in the first row and the corresponding permutations were indicated in the last row).

The Spearman coefficient (r) is computed by the following expression:

$$r = 1 - \frac{6 \sum_{i=1}^N D_i^2}{N(N^2 - 1)}, \quad (3)$$

TABLE 2: OM, SM, and the absolute error ($|\text{OM}-\text{SM}|$) in % for the 8 permutations.

Permutation	P1	P2	P3	P4	P5	P6	P7	P8
OM	44	35	59.7	41.7	56.9	29	68.1	58.3
SM	39.5	27.5	54.6	31.3	38.9	23.9	57.5	66
$ \text{OM}-\text{SM} $	4.5	7.5	5.1	10.4	18	5.1	10.6	7.7

TABLE 3: Rankings for SM, OM, and Beker score.

SM ranking	1	2	3	4	5	6	7	8
OM ranking	3	1	2	5	4	6	7	8
Beker ranking	3	1	5	6	8	3	7	2
Permutation	P8	P7	P3	P1	P5	P4	P2	P6

where D_i is the difference between the positions of the i th ranking and N is the size of the ranking (8 in the present case).

The values of r for both cases, between the OM and the SM and between Beker score and the SM, were computed (with D_i from Table 3) and the results were 0.9048 and 0.2024, respectively. These results show a strong correlation between the OM and the SM. In another experiment carried out by the authors with 23 permutable subbands, the Spearman coefficient obtained for the proposed measure, with respect to the subjective measure, was 0.9636, suggesting a higher correlation as the number of subbands increases. The Spearman coefficient of the Beker score was particularly low in this case; this results from the fact that the permutations used aimed to highlight the importance of each subband. It is worth mentioning that the score does not take into account which subbands are kept in their original positions; permutations $[1\ 2\ 3\ 4\ 8\ 7\ 6\ 5]^T$ and $[4\ 3\ 2\ 1\ 5\ 6\ 7\ 8]^T$, for example, have the same Beker score, but if we listen to a signal ciphered by them, the resulting intelligibilities are quite different (note that the first subband, due to the high probability of having the first formant, has a higher weight and is more intelligible if kept unaltered).

6. CONCLUSION

A new objective measure is proposed to evaluate the degree of intelligibility of a signal having its subbands permuted by a frequency domain scrambler. The measure can be used to generate efficient keys for frequency scramblers as well as to assess the performance of cryptanalysis schemes. All values presented in our simulations were specially tailored for this particular experiment: 8 subbands and Portuguese language.

REFERENCES

- [1] N. S. Jayant, "On the effective number of keys in a voice, privacy system based on permutation scrambling," *AT&T Technical Journal*, vol. 66, no. 1, pp. 192–196, 1987.
- [2] S. Sridharan, E. Dawson, and B. Goldberg, "Fast Fourier transform based speech encryption system," *IEE Proceedings I*, vol. 138, no. 3, pp. 215–223, 1991.

- [3] H. J. Beker and F. C. Piper, *Secure Speech Communications*, Academic Press, Boston, Mass, USA, 1985.
- [4] D. Klatt, "Prediction of perceived phonetic distance from critical-band spectra: a first step," in *Proceedings of the IEEE International Conference on Acoustics, Speech, and Signal Processing (ICASSP '82)*, vol. 7, pp. 1278–1281, Paris, France, May 1982.